

## Linear and Fuzzy Control Extensions of the Symmetrical Optimum Method

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**Abstract:** This paper deals with theoretical and applicative aspects concerning two extensions of the Symmetrical Optimum method (SO-m) for controller design focusing on speed and position control in mechatronics systems. The methods, introduced by the authors and called the Extended form of the Symmetrical Optimum method (ESO-m) and the Double parameterization of the Symmetrical Optimum method (2p-SO-m), are briefly presented. Due to the large applicability of the methods the authors elaborate and present some extensions to controllers with non-homogenous information processing with respect to the inputs and to fuzzy control solutions applications. Since the classical control algorithms are present in their different forms in a lot of practical applications (for example, in the electrical driving systems) the highlighted aspects are of permanent actuality.

**Keywords:** Double parameterization of the Symmetrical Optimum method, Extended form of the Symmetrical Optimum method, fuzzy control, mechatronics systems, non-homogenous dynamics.

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